CSC2515 Lecture 6: Convolutional Networks

David Duvenaud

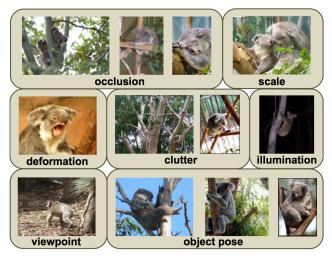
Based on Materials from Roger Grosse, University of Toronto

- Midterm grades this weekend
- Drop date March 1st
- HW3 released this weekend

- People are very good at recognizing shapes
 - Intrinsically difficult, computers are bad at it
- Why is it difficult?

Why is it a Problem?

• Difficult scene conditions



[From: Grauman & Leibe]

Why is it a Problem?

• Huge within-class variations. Recognition is mainly about modeling variation.



[Pic from: S. Lazebnik]

Why is it a Problem?

• Tons of classes

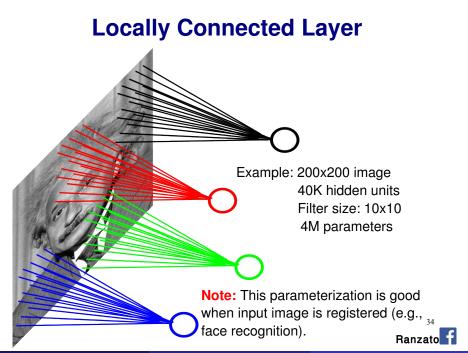


[Biederman]

- People are very good at recognizing object
 - Intrinsically difficult, computers are bad at it
- Some reasons why it is difficult:
 - Segmentation: Real scenes are cluttered
 - Invariances: We are very good at ignoring all sorts of variations that do not affect class
 - Deformations: Natural object classes allow variations (faces, letters, chairs)
 - A huge amount of computation is required

- How can we apply neural nets to images?
- Images can have millions of pixels, i.e., x is very high dimensional
- How many parameters do I have?

- How can we apply neural nets to images?
- Images can have millions of pixels, i.e., x is very high dimensional
- How many parameters do I have?
- Prohibitive to have fully-connected layers
- What can we do?
- We can use a locally connected layer



When Will this Work?

• This is good when the input is (roughly) registered



General Images

• The object can be anywhere



[Slide: Y. Zhu]

General Images

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[Slide: Y. Zhu]

General Images

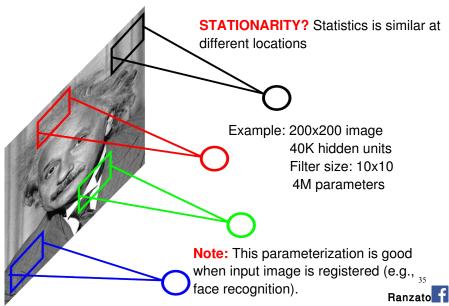
• The object can be anywhere



[Slide: Y. Zhu]

- Our perceptual systems are very good at dealing with invariances
 - translation, rotation, scaling
 - deformation, contrast, lighting
- We are so good at this that it's hard to appreciate how difficult it is
 - It's one of the main difficulties in making computers perceive
 - We still don't have generally accepted solutions

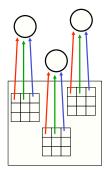
Locally Connected Layer



The replicated feature approach

5

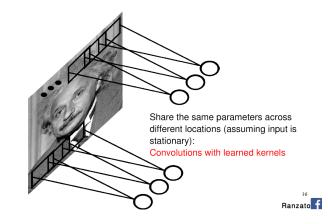
The red connections all have the same weight.



- Adopt approach apparently used in monkey visual systems
- Use many different copies of the same feature detector.
 - Copies have slightly different positions.
 - Could also replicate across scale and orientation.
 - Tricky and expensive
 - Replication reduces the number of free parameters to be learned.
- Use several **different feature types**, each with its own replicated pool of detectors.
 - Allows each patch of image to be represented in several ways.

Convolutional Neural Net

- Idea: statistics are similar at different locations (Lecun 1998)
- Connect each hidden unit to a small input patch and share the weight across space
- This is called a convolution layer and the network is a convolutional network

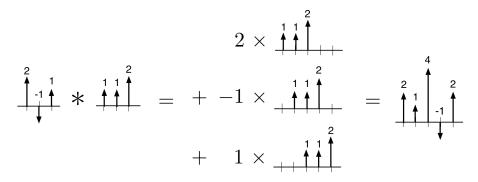


- Convolution layers are named after the convolution operation.
- If a and b are two arrays,

$$(a * b)_t = \sum_{\tau} a_{\tau} b_{t-\tau}.$$

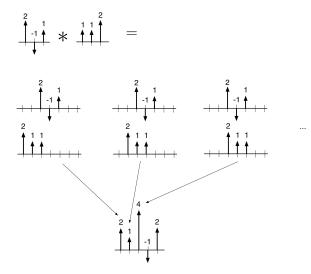
Convolution

Method 1: translate-and-scale



Convolution

Method 2: flip-and-filter



Convolution can also be viewed as matrix multiplication:

$$(2,-1,1)*(1,1,2)=egin{pmatrix} 1&1\ 1&1\ 2&1&1\ &2&1\ &2&1\ &2&1\ &2&1\ &2\end{pmatrix}egin{pmatrix} 2\ -1\ 1\end{pmatrix}$$

Aside: This is how convolution is typically implemented. (More efficient than the fast Fourier transform (FFT) for modern conv nets on GPUs!)

Some properties of convolution:

• Commutativity

a * b = b * a

Linearity

$$a*(\lambda_1b+\lambda_2c)=\lambda_1a*b+\lambda_2a*c$$

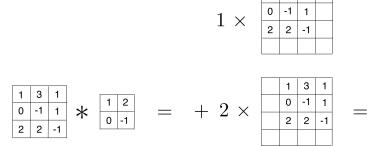
2-D convolution is defined analogously to 1-D convolution.

If A and B are two 2-D arrays, then:

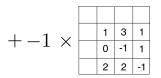
$$(A * B)_{ij} = \sum_{s} \sum_{t} A_{st} B_{i-s,j-t}.$$

2-D Convolution

Method 1: Translate-and-Scale



1	5	7	2	
0	-2	-4	1	
2	6	4	-3	
0	-2	-2	1	

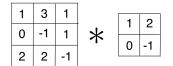


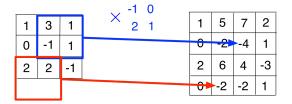
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Intro	ML ((UofT)

Method 2: Flip-and-Filter





The thing we convolve by is called a kernel, or filter.

*

What does this filter do?



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 \ast

What does this filter do?





















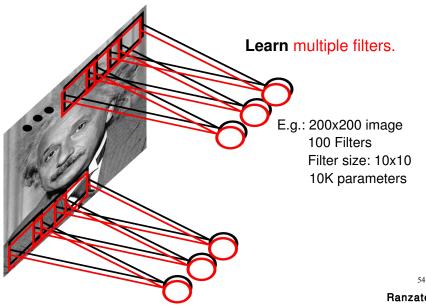


-1

-2

-1

Convolutional Layer



Convolutional Layer

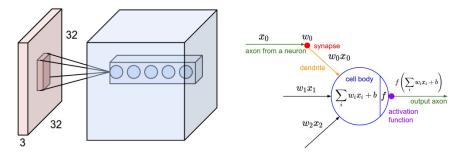
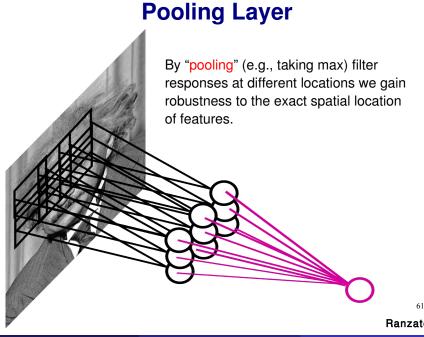


Figure: Left: CNN, right: Each neuron computes a linear and activation function

Hyperparameters of a convolutional layer:

- The number of filters (controls the **depth** of the output volume)
- The **stride**: how many units apart do we apply a filter spatially (this controls the spatial size of the output volume)
- The size $w \times h$ of the filters

[http://cs231n.github.io/convolutional-networks/]



- Max Pooling: return the maximal argument
- Average Pooling: return the average of the arguments
- Other types of pooling exist.

Pooling

224x224x64 Single depth slice 112x112x64 pool 2 4 1 1 х max pool with 2x2 filters 5 7 6 8 and stride 2 3 2 1 0 1 2 3 4 112 224 downsampling 112 V 224

Figure: Left: Pooling, right: max pooling example

Hyperparameters of a pooling layer:

- The spatial extent F
- The stride

[http://cs231n.github.io/convolutional-networks/]

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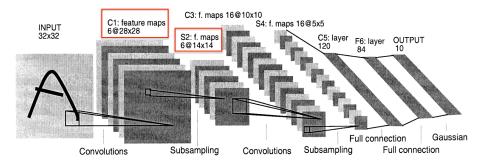
3 4

- The backprop procedure from last lecture can be applied directly to conv nets.
- This is covered in csc2516.
- As a user, you don't need to worry about the details, since they're handled by automatic differentiation packages.

• MNIST dataset of handwritten digits

- Categories: 10 digit classes
- **Source:** Scans of handwritten zip codes from envelopes
- ► Size: 60,000 training images and 10,000 test images, grayscale, of size 28 × 28
- Normalization: centered within in the image, scaled to a consistent size
 - The assumption is that the digit recognizer would be part of a larger pipeline that segments and normalizes images.
- In 1998, Yann LeCun and colleagues built a conv net called LeNet which was able to classify digits with 98.9% test accuracy.
 - It was good enough to be used in a system for automatically reading numbers on checks.

Here's the LeNet architecture, which was applied to handwritten digit recognition on MNIST in 1998:



- Ways to measure the size of a network:
 - Number of units. This is important because the activations need to be stored in memory during training (i.e. backprop).

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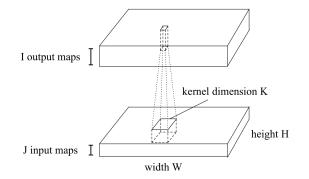
- ▶ Number of units. This is important because the activations need to be stored in memory during training (i.e. backprop).
- Number of weights. This is important because the weights need to be stored in memory, and because the number of parameters determines the amount of overfitting.

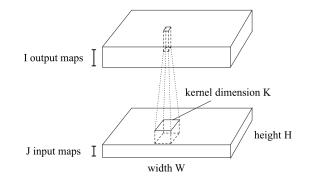
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- ▶ Number of connections. This is important because there are approximately 3 add-multiply operations per connection (1 for the forward pass, 2 for the backward pass).

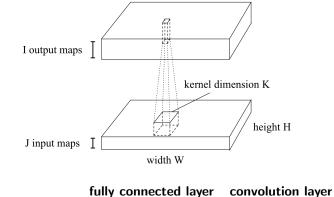
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- ▶ Number of connections. This is important because there are approximately 3 add-multiply operations per connection (1 for the forward pass, 2 for the backward pass).
- We saw that a fully connected layer with *M* input units and *N* output units has *MN* connections and *MN* weights.
- The story for conv nets is more complicated.



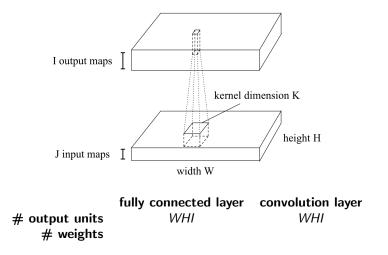


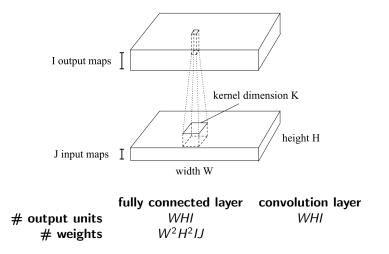
fully connected layer convolution layer # output units

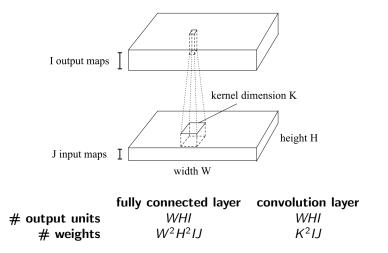


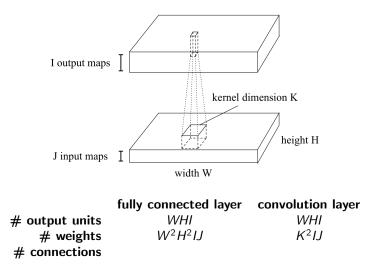
output units WHI

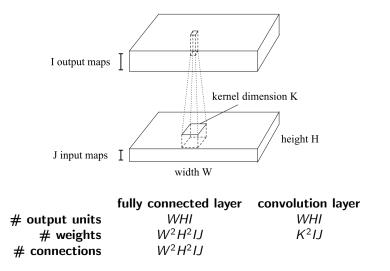
WHI

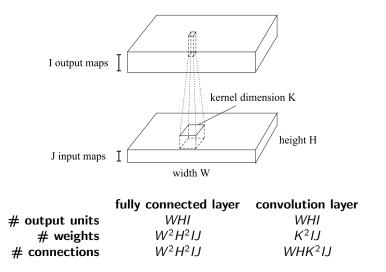












Sizes of layers in LeNet:

Layer	Туре	# units	# connections	# weights
C1	convolution	4704	117,600	150
S2	pooling	1176	4704	0
C3	convolution	1600	240,000	2400
S4	pooling	400	1600	0
F5	fully connected	120	48,000	48,000
F6	fully connected	84	10,080	10,080
output	fully connected	10	840	840

Conclusions?

- Rules of thumb:
 - Most of the units and connections are in the convolution layers.
 - Most of the weights are in the fully connected layers.
- If you try to make layers larger, you'll run up against various resource limitations (i.e. computation time, memory)
 - Conv nets have gotten a LOT larger since 1998!

ImageNet

ImageNet is the modern object recognition benchmark dataset. It was introduced in 2009, and has led to amazing progress in object recognition since then.

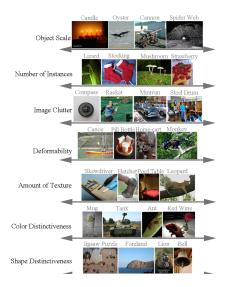
> ILSVRC flamingo cock ruffed grouse quail partridge Persian cat Siamese cat tabby Egyptian cat lynx dalmatian

keeshond miniature schnauzer standard schnauzer giant schnauzer

ImageNet

- Used for the ImageNet Large Scale Visual Recognition Challenge (ILSVRC), an annual benchmark competition for object recognition algorithms
- Design decisions
 - Categories: Taken from a lexical database called WordNet
 - WordNet consists of "synsets", or sets of synonymous words
 - They tried to use as many of these as possible; almost 22,000 as of 2010
 - Of these, they chose the 1000 most common for the ILSVRC
 - The categories are really specific, e.g. hundreds of kinds of dogs
 - Size: 1.2 million full-sized images for the ILSVRC
 - Source: Results from image search engines, hand-labeled by Mechanical Turkers
 - Labeling such specific categories was challenging; annotators had to be given the WordNet hierarchy, Wikipedia, etc.
 - Normalization: none, although the contestants are free to do preprocessing

Images and object categories vary on a lot of dimensions



Russakovsky et al.

Size on disk:

MNIST 60 MB

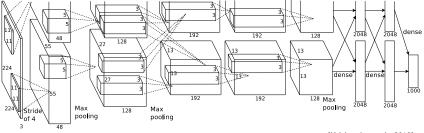
ImageNet 50 GB





AlexNet

• AlexNet, 2012. 8 weight layers. 16.4% top-5 error (i.e. the network gets 5 tries to guess the right category).



⁽Krizhevsky et al., 2012)

- The two processing pathways correspond to 2 GPUs. (At the time, the network couldn't fit on one GPU.)
- AlexNet's stunning performance on the ILSVRC is what set off the deep learning boom of the last 6 years.

Inception

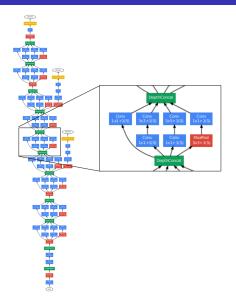
Inception, 2014. ("We need to go deeper!")

22 weight layers

Fully convolutional (no fully connected layers)

Convolutions are broken down into a bunch of smaller convolutions

6.6% test error on ImageNet



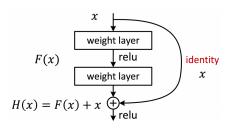
(Szegedy et al., 2014)

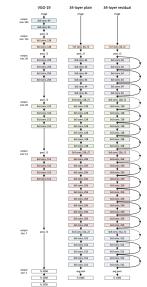
Inception

- They were really aggressive about cutting the number of parameters.
 - Motivation: train the network on a large cluster, run it on a cell phone
 - Memory at test time is the big constraint.
 - Having lots of units is OK, since the activations only need to be stored at training time (for backpropagation).
 - Parameters need to be stored both at training and test time, so these are the memory bottleneck.
 - How they did it
 - No fully connected layers (remember, these have most of the weights)
 - Break down convolutions into multiple smaller convolutions (since this requires fewer parameters total)
 - Inception has "only" 2 million parameters, compared with 60 million for AlexNet
 - This turned out to improve generalization as well. (Overfitting can still be a problem, even with over a million images!)

150 Layers!

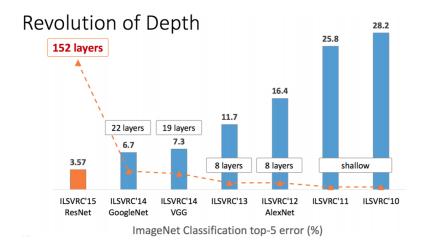
- Networks are now at 150 layers
- They use a skip connections with special form
- In fact, they don't fit on this screen
- Amazing performance!
- A lot of "mistakes" are due to wrong ground-truth





[He, K., Zhang, X., Ren, S. and Sun, J., 2015. Deep Residual Learning for Image Recognition. arXiv:1512.03385, 2016]

Intro ML (UofT)

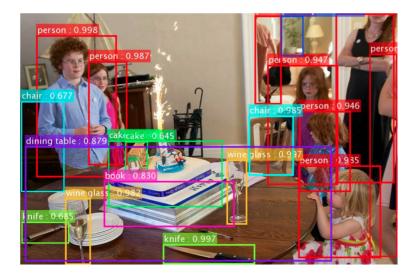


Slide: R. Liao, Paper: [He, K., Zhang, X., Ren, S. and Sun, J., 2015. Deep Residual Learning for Image Recognition. arXiv:1512.03385, 2016]

Intro ML (UofT)

CSC2515 Lec6

Results: Object Detection

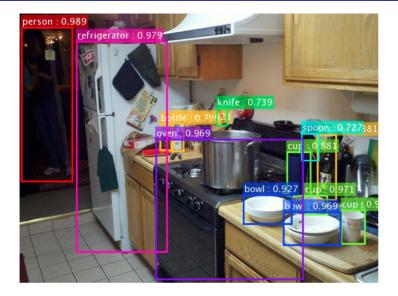


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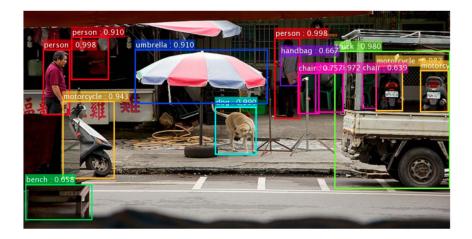
CSC2515 Lec6

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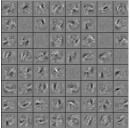
Results: Object Detection



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• Recall: we can understand what first-layer features are doing by visualizing the weight matrices.

Fully connected (MNIST)



Convolutional (ImageNet)



- Higher-level weight matrices are hard to interpret.
- The better the input matches these weights, the more the feature activates.
 - Obvious generalization: visualize higher-level features by seeing what inputs activate them.

- One way to formalize: pick the images and locations in the training set which activate a unit most strongly.
- Here's the visualization for layer 1:



• Layer 3:



• Layer 4:



Intro ML (UofT)

CSC2515 Lec6

• Layer 5:



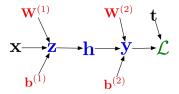


- Higher layers seem to pick up more abstract, high-level information.
- Problems?

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- Problems?
 - Can't tell what the unit is actually responding to in the image.
 - We may read too much into the results, e.g. a unit may detect red, and the images that maximize its activation will all be stop signs.

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- Problems?
 - Can't tell what the unit is actually responding to in the image.
 - We may read too much into the results, e.g. a unit may detect red, and the images that maximize its activation will all be stop signs.
- Can use input gradients to diagnose what the unit is responding to.
 - Optimize an image from scratch to increase a unit's activation

• Recall the computation graph:



• From this graph, you could compute $\partial \mathcal{L}/\partial x,$ but we never made use of this.

- Can do gradient ascent on an image to maximize the activation of a given neuron.
- Requires a few tricks to make this work; see https://distill.pub/2017/feature-visualization/

Starting from random noise, we optimize an image to activate a particular neuron (layer mixed4a, unit 11).



Step 0



Step 4



Step 48



Step 2048

Optimizing the Image

Dataset Examples show us what neurons respond to in practice

Optimization isolates the causes of behavior from mere correlations. A neuron may not be detecting what you initially thought.



Baseball—or stripes? mixed4a, Unit 6

Animal faces—or snouts? mixed4a, Unit 240

Clouds—or fluffiness? B mixed4a, Unit 453 m

Buildings—or sky? mixed4a, Unit 492

• Higher layers in the network often learn higher-level, more interpretable representations



https://distill.pub/2017/feature-visualization/

Optimizing the Image

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Parts (layers mixed4b & mixed4c)

Objects (layers mixed4d & mixed4e)

https://distill.pub/2017/feature-visualization/